

Electronic Structure of AIP Under Pressure Using Semiempirical Method

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Abstract: The effect of pressure on the structural and electronic parameters of zinc-blende aluminum phosphide crystal has been investigated using the large unit cell within the framework of complete neglect of differential overlap and the linear combination of atomic orbital approximation. Cohesive energy, indirect band gap, valence bandwidth, conduction bandwidth, bulk modulus, and valence charge distribution are all obtained. The calculations show a good agreement of lattice constant, cohesive energy, valence bandwidth, and bulk modulus with the experimental data. The calculated band gap is twice the experimental value. This high value of the band gap is expected in Hartree-Fock method. The effect of pressure on the aforementioned properties is investigated. It is found that the indirect band gap, valence bandwidth, bulk modulus and cohesive energy increase with increasing pressure, while the conduction bandwidth decreases. The maximum value of pressure is taken to be 9 GPa, because beyond this value, the phase of AIP transforms from zinc blende phase to nickel arsenic phase.

PACS: 71.10-w, 71.15-m, 71.15. Ap, 71.15. Nc, 64.10.+h.

Keywords: Pressure, band structure, AIP, semiempirical, LUC, CNDO.

1. INTRODUCTION

Aluminum phosphide (AIP) is a wide-indirect band gap semiconductor. At normal conditions, AIP crystallizes in the zinc-blende (zb) structure [1]. High-pressure experiments on this compound are difficult because of sample handling problems; AIP is unstable in air [2]. The zb form has been reported theoretically to be metastable. The zinc-blende phase is known to transform to the nickel arsenic (NiAs) phase at about (17 – 9.5 GPa [3]. Although other studies have placed this transformation at a somewhat smaller pressure (7 - 9.3) GPa [4]. At a pressure of about 36 GPa the NiAs phase has been reported to undergo a Cmc₂m-like distortion with no significant change in volume. The CsCl phase is a possible candidate for AIP at very high pressures [2]. AIP is a subject of extensive theoretical studies ranging from the semiempirical to the first principles methods [5] within the density functional theory (DFT) framework using both pseudopotential [2], and all-electron approaches. For the bulk phase of AIP, theoretical calculations based on the Hartree-Fock [6], and potential model [7] have obtained a very good description of its structural and electronic properties.

Over the last few years, the study of materials under high pressure has become an extremely important subject. This is primarily due to both theoretical and experimental developments, which have facilitated such work [8].

The pressure is a continuously varying parameter that can be used in systematic studies of the properties of solids as a function of interatomic distances. An interesting phenomenon that may occur at the applied pressure is a sudden change in the arrangement of the atoms, i.e., a structural phase transition of atomic arrangement. The ultimate pressures in the experiment can lead to a reduction in the volume by a factor of two causing enormous changes in the interatomic bonding [9].

In the present work we study the band structure and some physical properties of cubic AIP under pressure using large unit cell method within complete neglect of differential overlap (LUC-CNDO) method [10, 11]. This method has been chosen in the present work rather than other methods because this can be used to give reliable and precise results with relatively short time.

2. CALCULATIONS

We have used the large unit cell within complete neglect of differential overlap (LUC-CNDO) method in the linear combination of atomic orbital (LCAO) approximation [10] to obtain a self-consistent solution for the valence electron energy spectrum. The iteration process was repeated until the calculated total energy of crystal converged to less than 1meV. The calculations are carried out, on the 8-atom LUC. The positions of atoms that constitute this LUC are calculated in the program according to the zinc-blende structure for a given lattice constant. There are four electrons in average per each atom. Hence we have (32) eigenstates, two

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electrons per state, half are filled (valence band) leaving the other half empty (conduction band) in the ground state. We obtained the energy minima against lattice constant variation.

The basic idea of the large unit cell is in computing the electronic structure of the unit cell extended in a special manner at $\mathbf{k}=0$ in the reduced Brillouin zone (\mathbf{k} is the lattice wave vector). Using the linear combination of atomic orbitals LCAO, the crystal wavefunction in the LUC-CNDO formalism is written in the following form [12]:

$$\psi_a(\mathbf{k}, r) = \sum_u \sum_p^{\text{cells basis}} \exp(i\mathbf{k}R_u) C_{pa}(\mathbf{k}) \varphi_p(r - R_u) \quad (1)$$

where C_{pa} are the orbital expansion coefficients, the R_u is the lattice translation vector, and r is a position vector. The atomic orbitals used for the LCAO procedure form the basis set of the calculation. We expand the wave function in a set of Slater-type orbitals (STO), that have the radial form [13]:

$$R_{nl}(r) = \frac{(2\zeta)^{n+1/2}}{(2n!)^{1/2}} r^{n-1} \exp(-\zeta r) \quad (2)$$

where ζ the orbital exponent. The expectation value of the electronic energy is:

$$\varepsilon = \langle \Psi | H | \Psi \rangle / \langle \Psi | \Psi \rangle \quad (3)$$

The Hamiltonian for a microcrystal consisting of N electrons may be written as:

$$H = \sum_a^N \left(-\frac{1}{2} \nabla_a^2 - \sum_A^{n_A} Z_A r_{AA}^{-1} \right) - \frac{1}{2} \sum_a^N \sum_p^N r_{ap}^{-1} + \sum_A^{n_A} \sum_B^{n_B} Z_A Z_B R_{AB}^{-1} \quad (4)$$

where Z_A is the core charge, R_{AB} is the distance between the atoms A and B, and the summation is over all nuclei. The Roothaan-Hall equations can be obtained [14]:

$$\sum_p (F_{pqk} - \varepsilon_a S_{pqk}) C_{pqk} = 0 \quad (5)$$

F_{pqk} represents the Fock matrix elements. S_{pq} is the overlap integral for atomic function φ_q and φ_p , and can be written as [12]:

$$S_{pqk} = \sum_u \langle \varphi_p(r - R_0) | \varphi_q(r - R_u) \rangle \exp(i\mathbf{k}R_u) \quad (6)$$

The Fock matrix elements may represent the sum of the one- and two- electron components:

$$F_{op,uq} = \left\langle \varphi_p^1(1) \left| -\frac{1}{2} \nabla_1^2 - \sum_a Z_a r_{1a}^{-1} \right| \varphi_q^u(1) \right\rangle + \sum_{v,\lambda}^{\text{cell basis}} \sum_{rs} P_{rs}^{v\lambda} ((\varphi_p^o \varphi_q^u | \varphi_r^v \varphi_s^\lambda) - \frac{1}{2} (\varphi_p^o \varphi_r^v | \varphi_s^\lambda \varphi_q^u)) \quad (7)$$

$P_{rs}^{v\lambda}$ is the density element with the form:

$$P_{rs}^{v\lambda} = 2 \sum_{k'} \sum_a^{\text{occ}} C_{rak'}^* C_{sak'} \exp i\mathbf{k}' \cdot (R_\lambda - R_v) \quad (8)$$

In equation (5) if $\mathbf{k}=0$ then

$$\sum_p (F_{pq0} - \varepsilon_a S_{pq0}) C_{pq0} = 0 \quad (9)$$

The Fock matrix elements in their final forms in the LUC-CNDO formalism are used in this work to be [11]:

$$F_{pp}(0) = -\frac{1}{2} (I_p + A_p) + \frac{1}{2} \gamma_{AA}^{00} + \sum_B (P_B(0) - Z_B) \sum_v \gamma_{AB}^{0v} + \sum_{v \neq 0} \beta_{AB}^{0v} S_{0p,vp} - \frac{1}{2} \sum_{v \neq 0} P_{pp}(0) f(x) \gamma_{AA}^{0v} \quad (10)$$

$$F_{pq(0)} = \sum_v \beta_{AB}^0 S_{op,vp} - \frac{1}{2} P_{pq}(0) \sum_v f(x) \gamma_{AB}^{0v} \quad (11)$$

For p and q on the same atomic center, β_{AB} is the bonding parameter and γ_{AB} is the average electrostatic repulsion between any electron on atom A and any electron on atom B, and can be written as

$$\gamma_{AB} = \iint \varphi_p(1) \varphi_q(1) \frac{1}{r_{12}} \varphi_p(2) \varphi_q(2) d\tau_1 d\tau_2 \quad (12)$$

I_p and A_p are the ionization potential and electron affinity respectively, and $f(x)$ is the modulating function that is given by [15]

$$f(x) = \left(\frac{\sin(x)}{x} \right)^2 \quad (13)$$

For the eight atoms LUC x is given by

$$x = \frac{\pi R_{AB}}{a} \quad (14)$$

R_{AB} is the distance between the atom A at the central lattice o and the atom B at the v lattice.

In our calculations, we have treated only valence orbitals of Al ($3s^2 3p^1$) and P ($3s^2 3p^3$). The coordinates of the P atoms are chosen to be (0, 0, 0); (0, 1/2, 1/2); (1/2, 0, 1/2); (1/2, 1/2, 0) whereas the coordinates of the Al atoms are chosen to be (1/4, 1/4, 1/4); (1/4, 3/4, 3/4); (3/4, 1/4, 3/4); (3/4, 3/4, 1/4).

3. RESULTS AND DISCUSSION

3.1. Choice of Parameters

The number of parameters in the LUC-CNDO method is four. These are the orbital exponent (ζ), the bonding parameter (β), the electronegativity of s-orbital (E_s), and the electronegativity of p-orbital (E_p). The value of the orbital exponent determines the charge distribution of electrons around the nucleus in the solid

These parameters are varied firstly to give nearly an exact value of the equilibrium lattice constant, cohesive energy,

indirect bandgap and valence bandwidth. The remaining of the output data of the programs is a result of the theory that is used in the present work. We found that the investigated properties are sensitive to the aforementioned parameters. The parameters used for AIP in the present work are summarized in Table 1.

Table 1. The Adjusted Parameters for AIP in the Zinc-Blende Structure

Parameter	Al	P
$\zeta_{3s,3p}(\text{a.u.})^{-1}$	1.4	2.0
β (eV)	-6.0	-4.82
E_{3s} (eV)	9.75	24.58
E_{3p} (eV)	8.68	12.086

3.2. The Electronic and Structural Properties

The second step after the choice of parameters is to examine the structural properties of AIP at the equilibrium lattice constant in order to test the accuracy of the cohesive energy, indirect bandgap, and valence bandwidth.

Based on the total energy result, we obtained the cohesive energy (E_{coh}) as follows:

$$E_{\text{coh}} = E_{\text{tot}}/8 - E_{\text{free}} - E_0 \quad (15)$$

where E_{tot} is the total energy, E_{free} is the free atom sp shell energy, and E_0 is the zero-point vibration energy. In the present work $E_{\text{free}} = 115.045 \text{ eV}$, and this value is taken from the ionization potential of AIP, $E_0 = 0.057 \text{ eV}$, is calculated by the formula $E_0 = (9/8)k_B\Theta_D$ (per atom) with Θ_D is the Debye temperature [16], which is equal to 588 K [17].

The present value of the cohesive energy is in good agreement with the experimental and other calculations [16,18,19] as shown in Table 2. Fig. (1) displays the total energy versus the lattice constant for AIP. The curve is fitted to the equation of state of Murnaghan [20] from which we obtained the equilibrium lattice parameter (a_0), the bulk modulus B and its derivative B'_0 , and the cohesive energy as listed in Table 2.

The calculated structural properties of AIP, in comparison with experimental results and other computational results, are shown in Table 2. We notice that the lattice

parameter for the zb of AIP of 5.453 \AA is in good agreement with the experimental value of 5.451 \AA [6] with an accuracy of 0.04%. For the bulk modulus, the accuracy is about 0.2%. Table 2 shows that the calculated value of B'_0 is in fair agreement with the previous computational [4, 19] and experimental [18] results.

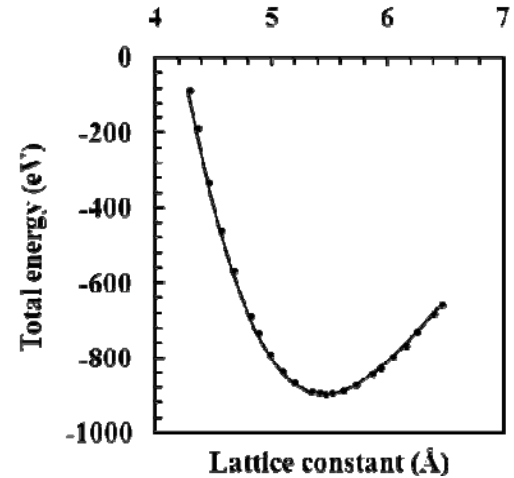


Fig. (1). The total energy as a function of lattice constant for AIP.

To visualize the nature of the bond character and to explain the charge transfer and the bonding properties of zb-AIP, we calculate the total charge density. The total valence charge densities for AIP are displayed along the Al-P bonds in the (100), (110), (200), and (400) planes in Fig. (2). From this figure, it is apparent that the phosphorous ions are larger than the aluminum ions. This figure also shows the charge density accumulated at the P site. Fig. (2a) shows the charge density of the (100) plane, where a buildup of charge density along the AIP bond on the plane is clearly visible. This figure reveals that LUC-CNDO calculations give a reasonable description of the partially ionic bonding character in regions between atoms of different affinities.

3.3. The Band Structure and Energy Eigenvalues

The electronic band structure of a solid shows the eigenvalues associated with the valence and conduction bands along specific directions in the Brillouin zone. We will start our discussion of calculations on the band structure by the energy eigenvalues for AIP crystal at various high symmetry points of the Brillouin zone. The results are listed in Table 3. Eight atom LUC results Γ and X points of the FCC Brillouin

Table 2. Structural Properties of zb-AIP at Zero Pressure Determined by LUC-CNDO Compared to other Theoretical Calculations and Experimental Data

	Present Work	Computational	Experimental
A_0 (Å)	5.453	5.45 [2], 5.436 [19]	5.451 [6]
E_{coh} (eV)	-8.33	-7.94 [16], -9.62 [19]	-8.34 [18]
B (GPa)	87.8	86.5 [4], 89 [19]	90 [2], 86 [6]
B'_0	3.852	4.18 [4], 4.14 [19]	4.34 [18]

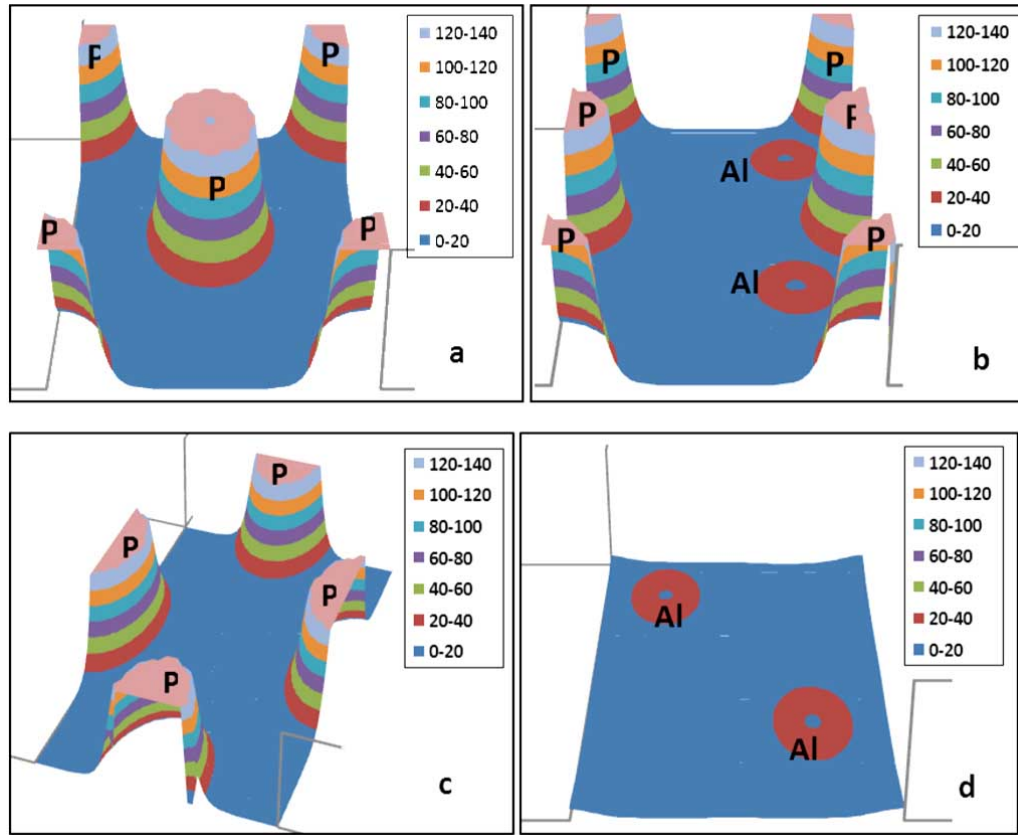


Fig. (2). The valence charge density (in electron/Å³) of zb-AIP at zero pressure in (a) (100) plane, (b) (110) plane, (c) (200) plane, and (d) (400) plane.

zone. They are the valence band states Γ_{1v} , Γ_{15v} , X_{1v} , and X_{5v} , and the conduction band states X_{1c} , X_{5c} , Γ_{15c} , and Γ_{1c} .

The direct bandgap in the zb structures of AIP is due to the Al 3s and P 3s orbital interaction, which forms the lower-energy bonding state (Γ_{15v}) and the antibonding state (Γ_{1c}). The bonding state is lowered and antibonding states is risen, relative to the P 3s and Al 3s orbital energies, by the same amount of s-s interaction energy in AIP. In zb-AIP the conduction-band minimum (CBM) is located away from the Γ point, at the X point. AIP has an indirect minimum gap with the CBM at X. Thus, we obtain an indirect bandgap (E_g^{ind}) of 6.6075 eV which is larger than the results of others [21, 22] (see Table 4 for comparison), this is, mainly, a consequence of two approximations made in the present calculations. First, the core structure was ignored, through some compensation results from using semiempirical parameters. Second, using minimal basis set atomic orbitals (without considering any excited levels). However, the CNDO method predicts a one-electron eigenvalue band gap that is too large and conduction band that is much narrower than the band model values.

The total valence bandwidth (VBW) or the difference between the top of the valence band (Γ_{15v}) and the lowest energy of valence band (Γ_{1v}) is 13.492 eV for zb-AIP. The obtained total valence bandwidth is in fair agreement with previous results as shown in Table 4. The maximum level of the valence band is splitted only by spin-orbit interaction Δ_{so} , giving rise to two states at the Brillouin zone centre: Γ_{8v} and

Γ_{7v} . In the absence of spin orbit splitting, these levels become a triply degenerated Γ_{15v} . The spin-orbit interaction Δ_{so} is taken into account in this paper, averaging the theoretical results from different Refs. to be 0.06eV [21, 23, 24]. Therefore, we added the relativistic correction to the band gap, which is equal to 0.019 [23]. Our work gives a value of the conduction bandwidth (CBW) to be 14.728 eV (Table 4), but no experimental results are found to the CBW of the zb of AIP.

4. THE EFFECT OF PRESSURE ON THE PHYSICAL PROPERTIES

The effect of pressure on the electronic structure and other properties can be calculated from the present computational procedure. By the use of our calculated values of the bulk modulus B and its derivative B'_0 , the volume change (V) with applied pressure was calculated using the following equation [26]:

$$P = \frac{B_0}{B'_0} \left[\left(\frac{V_0}{V} \right)^{B'_0} - 1 \right] \quad (16)$$

P is the pressure and V_0 is the equilibrium volume at zero pressure. We use pressures up to 9 GPa, because this structure transforms to another phase, the nickel arsenic phase (NiAs), when pressure exceeds nearly 9 GPa [27]. The calculated lattice constant as a function of pressure is shown in Fig. (3).

conduction bandwidth decreases with the increase of pressure, while the valence bandwidth increases with the increase of pressure. Our calculations give a pressure derivative of ~ -1.9 meV/GPa for the conduction bandwidth, and 22 meV/GPa for the valence bandwidth.

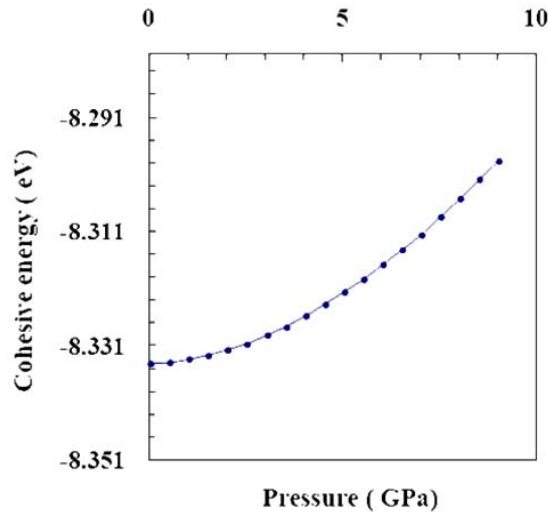


Fig. (5). The effect of pressure on the cohesive energy of AIP.

5. CONCLUSIONS

In this paper, a study of some properties of AIP is presented. The cohesive energy, lattice constant, bulk modulus, and its pressure derivative have been calculated by (LUC-CNDO) method. The calculated results indicate that this model gives results in good agreement with the corresponding experimental results, and this shows the possibility of using this model in qualitative study of some materials. The LUC-CNDO method is shown to be time efficient and retains many of the essential features of ab initio Hartree-Fock theory. A reasonable agreement of the valence band-

width is shown in comparison with the available theoretical result. However, there is a large difference between the calculated indirect band gap and the corresponding experimental value. The effect of pressure on these properties is investigated. It is found that the conduction bandwidth decreases with increasing the pressure, whereas the indirect bandgap, valence bandwidth, and cohesive energy increase with the increase of pressure. The maximum value of pressure is taken to be 9 GPa, because beyond this value of pressure, the phase of AIP transforms from zb to rock salt phase. Relativistic effect is added to the calculation of the band gap, also zero point energy is added to the calculation of the cohesive energy. Finally, this model is shown to give a good description to the charge density of AIP and it is expected that this method could give reliable description for other materials that have zinc blende and cubic structures.

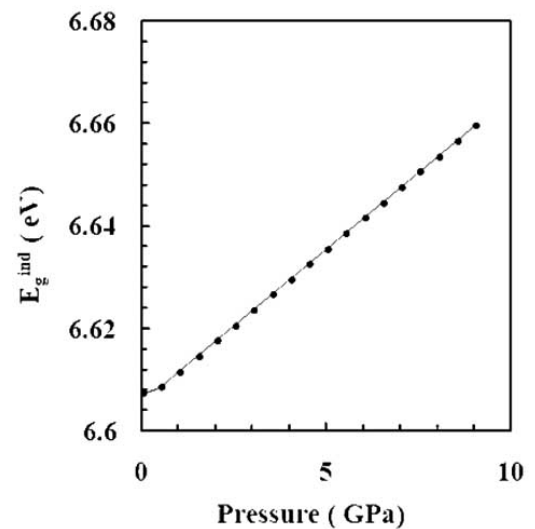


Fig. (7). Variation of the indirect band gap versus pressure for AIP.

Fig. (6). The effect of pressure on the high symmetry points in the (a) conduction band (X_{5c} , Γ_{15c} , Γ_{1c} , X_{1c}), and (b) valence band (X_{5v} , X_{1v} , Γ_{1v}).

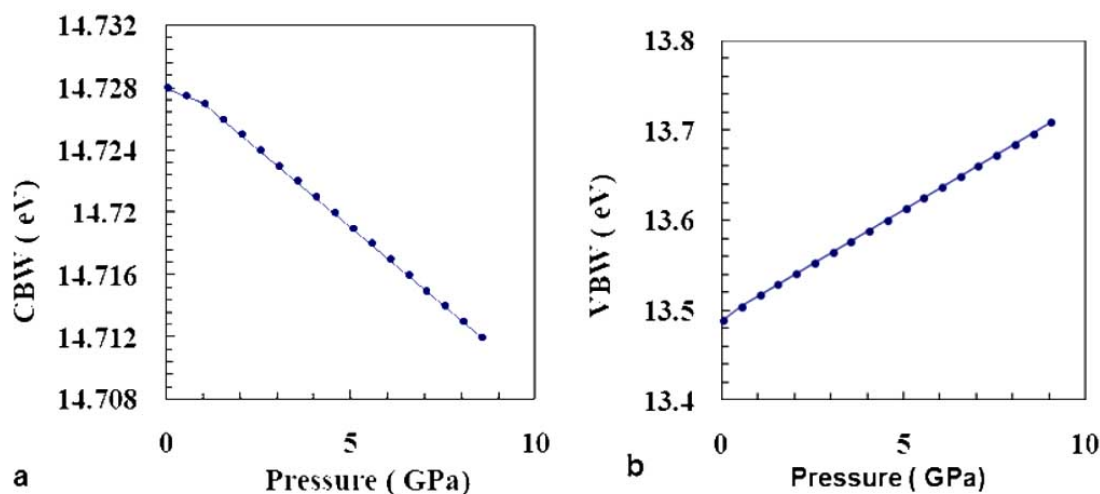


Fig. (8). Effect of pressure on the (a) conduction bandwidth, and (b) valence bandwidth.

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Received: August 21, 2009

Revised: October 11, 2009

Accepted: October 28, 2009

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