

Lecture -6-

2-1 Simple crystal structure

2-1-1 Sodium chloride structure (NaCl)

NaCl structure is shown in Fig.12

- The lattice is FCC
- The basis consists of 1 Na^+ ion and 1 Cl^- ion separated by $\frac{1}{2}$ the diagonal of a unit cube.
- There are 4 units in each unit cube.
- The coordination number of NaCl is 6
- The coordinates of atoms in unit cube are
 $0,0,0$; $\frac{1}{2},\frac{1}{2},0$; $\frac{1}{2},0,\frac{1}{2}$; $0, \frac{1}{2},\frac{1}{2}$
 $\frac{1}{2},\frac{1}{2},\frac{1}{2}$; $0,0, \frac{1}{2}$; $0, \frac{1}{2},0$; $\frac{1}{2},0,0$

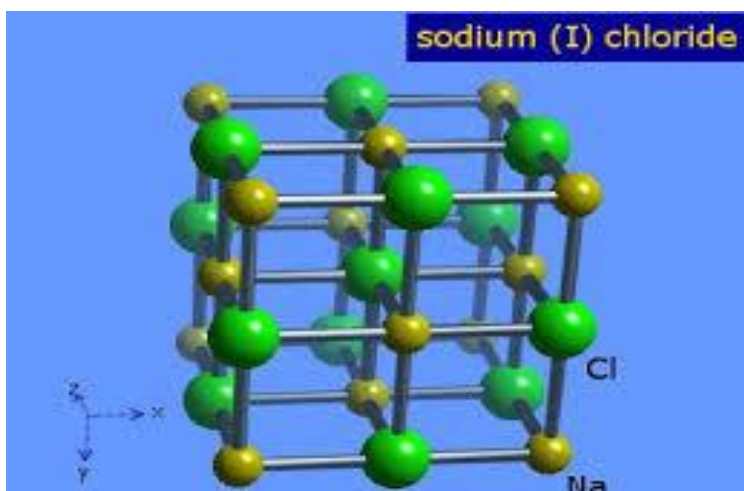


Fig.12 NaCl structure

2-1-2 Cesium chloride structure (CsCl)

ClCs structure is shown in Fig.13

- The lattice is BCC
- The basis has 1 Cs^+ ion at $0,0,0$ and 1 Cl^- ion at $\frac{1}{2},\frac{1}{2},\frac{1}{2}$
- The coordination number of CsCl is 8

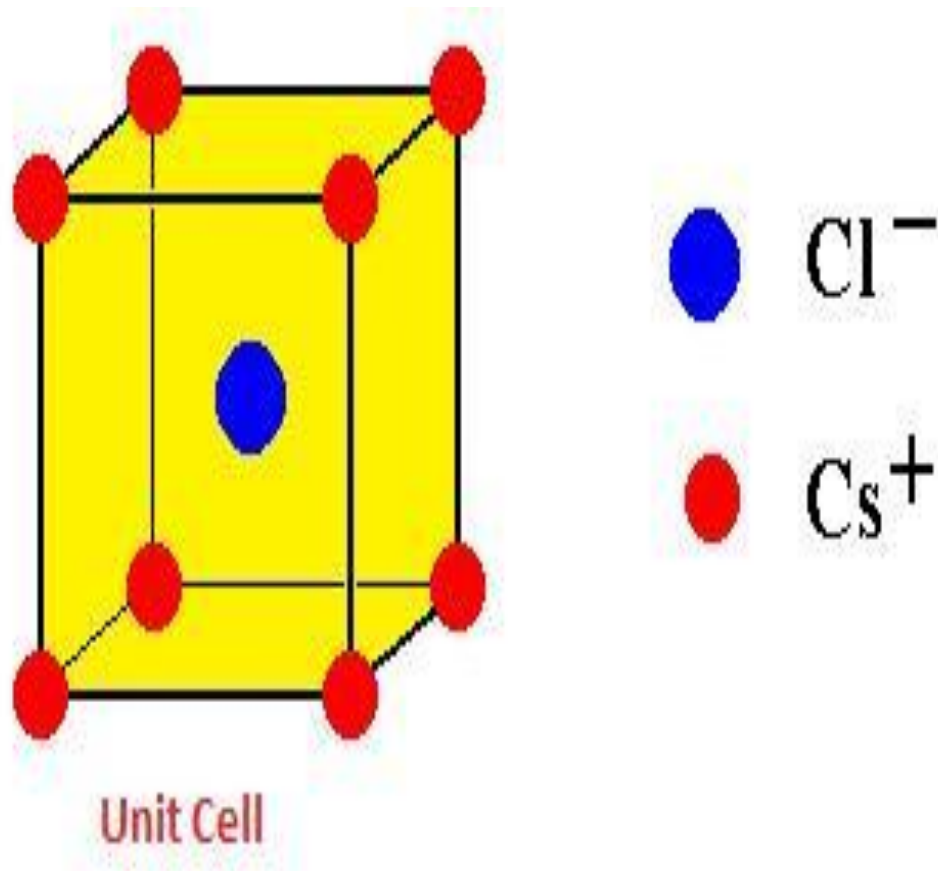


Fig.13 CsCl structure

2-1-3 Hexagonal close packed structure (hcp)

A close packed- layer of spheres (atoms) is shown in Fig. 14, with centers at points (A). A second layer goes in over (B). A third layer (C) may be added in two ways: if it goes in over (A) the order is AB ABAB and the structure is hcp (see Fig. 15).

Note:

The indices of the plane in hexagonal structure marked by (hkil), where $i = -(h+k)$

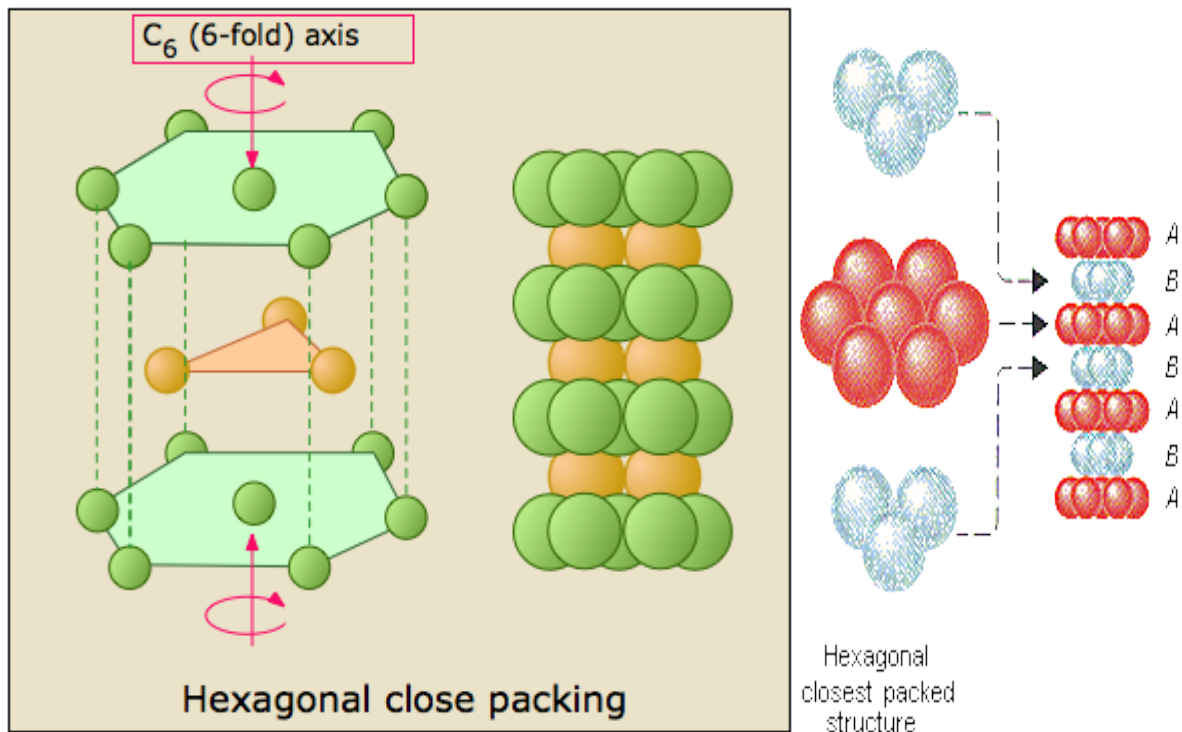


Fig.14

If it goes in over (C) the order is ABC ABC ABC and the structure is FCC.

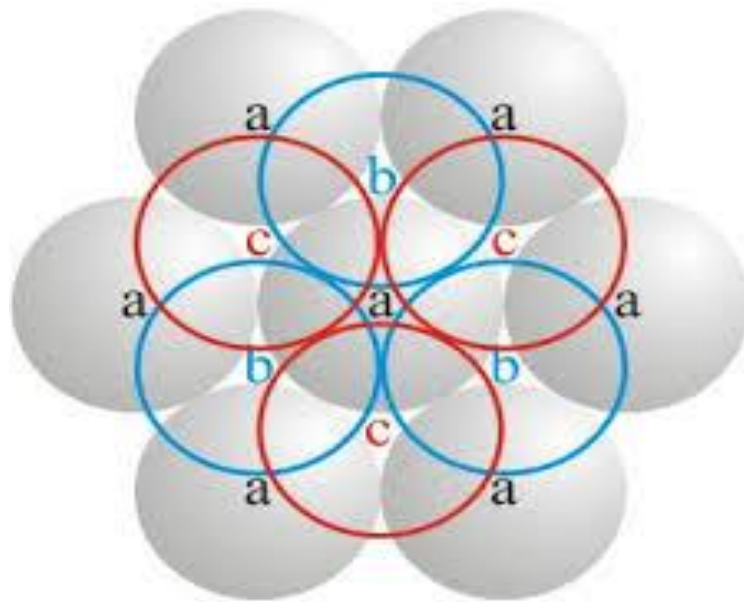
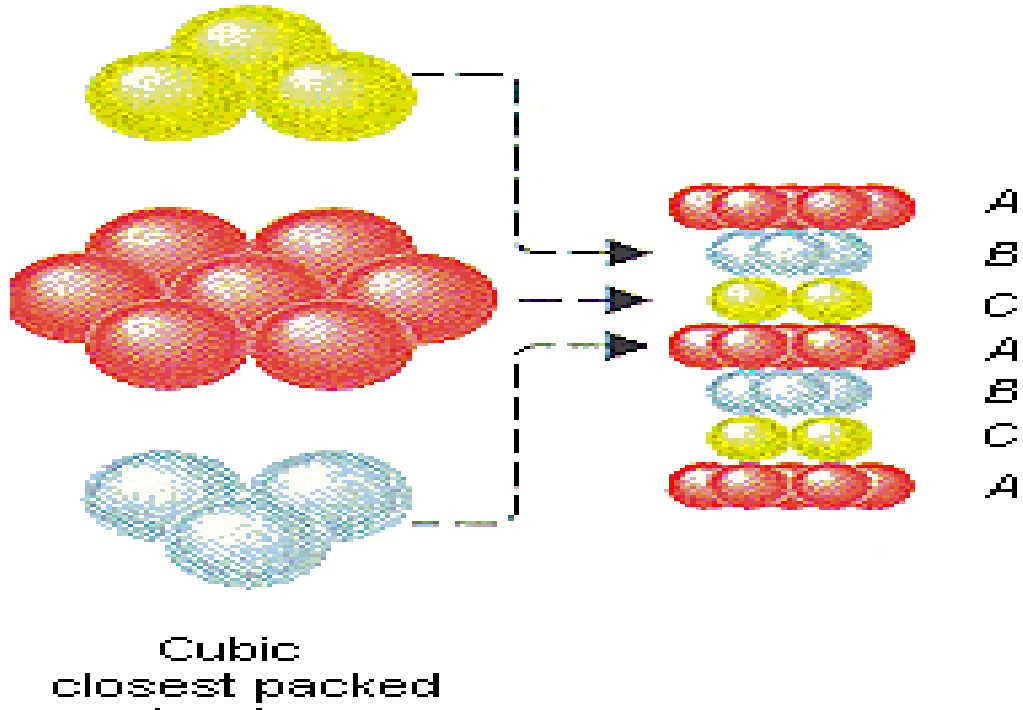


Fig. 15

2-1-4 Diamond structure

Diamond structure is shown in Fig.16

- The lattice is FCC
- The basis has 2 identical atoms at coordinates $0,0,0$ and $\frac{1}{4},\frac{1}{4},\frac{1}{4}$.
- The coordinates of atoms in unit cube are
 $0,0,0$; $\frac{1}{2},\frac{1}{2},0$; $\frac{1}{2},0,\frac{1}{2}$; $0, \frac{1}{2},\frac{1}{2}$
 $\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$; $\frac{3}{4}, \frac{3}{4}, \frac{1}{4}$; $\frac{3}{4}, \frac{1}{4}, \frac{3}{4}$; $\frac{1}{4}, \frac{3}{4}, \frac{3}{4}$
- The coordination number is 4

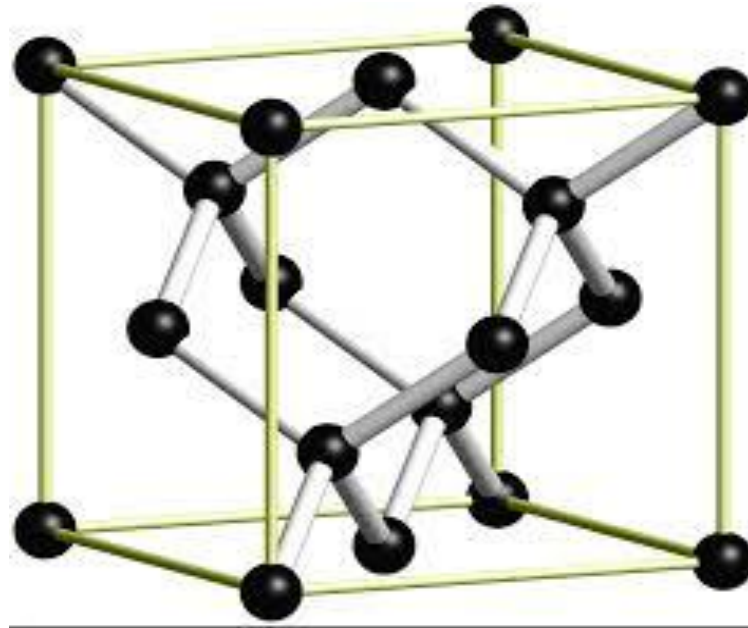


Fig.16 Diamond structure

1-12 Filling factor(or packing fraction)

Filling factor = space occupied by the atoms x
number of atoms per unit cell / total volume

① For SC

$$\text{Filling factor} = \frac{4}{3} \pi r^3 \times 1 / a^3 = \frac{4}{3} \pi \left(\frac{a}{2}\right)^3 \times 1 / a^3 = 52\%$$

② For BCC

$$\text{Filling factor} = \frac{4}{3} \pi r^3 \times 2 / a^3 = \frac{4}{3} \pi (\sqrt{3}a/4)^3 \times 2 / a^3 = 68\%$$

③ For FCC

$$\text{Filling factor} = \frac{4}{3} \pi r^3 \times 4 / a^3 = \frac{4}{3} \pi \left(\frac{a}{2\sqrt{2}}\right)^3 \times 4 / a^3 = 74\%$$

④ For Diamond structure

$$\text{Filling factor} = \frac{4}{3} \pi r^3 \times 8 / a^3 = \frac{4}{3} \pi \left(\sqrt{3} \frac{a}{8}\right)^3 \times 1 / a^3 = 34\%$$