

Mechanics : is a branch of the physical sciences that is concerned with the state of rest or motion of bodies that are subjected to the action of forces .

In general , this subject can be subdivided into three branches : **rigid-body mechanics**, **deformation-body mechanics**, and **fluid mechanics**.

We will study rigid-body mechanics since it is a basic requirement for the study of the mechanics of deformable bodies and the mechanics of fluid . Furthermore, rigid-body mechanics is essential for the design and analysis of many types of structural members and mechanical components .

Rigid-body mechanics is divided into two areas : statics and dynamics. Statics deals with the equilibrium of bodies , that is , those are either at rest or move with a constant velocity ; whereas dynamics is concerned with the accelerated motion of bodies.

Basic Quantities :

The following four quantities are used throughout mechanics.

Length :is used to locate the position of a point in space and thereby describe the size of physical system .

Time : is conceived as a succession of events .

Mass : is a measure of a quantity of matter that is used to compare the action of one body with that of another .

Force : is considered as a " push " or " pull" exerted by one body on another . This interaction can occur when there is direct contact between the bodies, such as a person pushing on a wall , or it can occur through a distance when the bodies are physically separated.

Idealizations :

Models or idealizations are used in mechanics in order to simplify application of the theory . Here we will consider three important idealizations :

Particle : a particle has a mass , but a size that can be neglected. When a body is idealized as a particle. The principles of mechanics reduce to a rather simplified form since the geometry of the body will not be involved in the analysis of the problem .

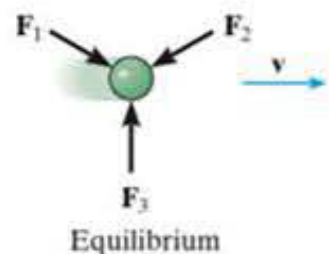
Rigid Body : a rigid body can be considered as a combination of a large number of particles in which all the particles remain at a fixed distance from one another , both before and after applying a load .

Concentrated Force : a concentrated force represents the effect of a loading which is assumed to act at a point on a body. We can represent a load by a concentrated force .

Newton's Three Laws of Motion :

Engineering mechanics is formulated on the basis of Newton's three laws of motion. The validity of which is based on experimental observation . These laws apply to the motion of particle as measured from a nonaccelerating reference frame. They may be briefly stated as follows :

First Law : A particle originally at rest , or moving in a straight line with constant velocity, tends to remain in this state provided the particle is not subjected to an unbalanced force.

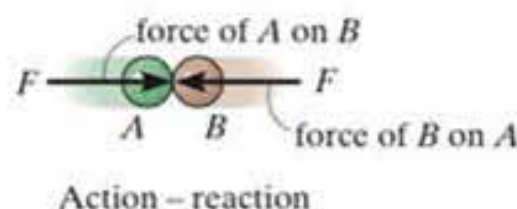


Second Law : A particle acted upon by an unbalanced force \mathbf{F} experiences an acceleration \mathbf{a} that has the same direction as the force and a magnitude that is directly proportional to the force . If \mathbf{F} is applied to a particle of mass \mathbf{m} , this law may be expressed mathematically as :

$$\mathbf{F} = m\mathbf{a}$$



Third Law : the mutual forces of action and reaction between two particles are equal, opposite , and collinear .



Units of Measurement :

SI Units : the International System of units, is a modern version of the metric system which has received worldwide recognition. The **SI** system defines length in meters (**m**), time in seconds (**s**), and mass in kilograms (**kg**). The unit of force, called a newton (**N**), is derived from **F = ma**. Thus, 1 Newton is equal to a force required to give 1 kilogram of mass an acceleration of **1 m/s²** (**N = kg.m/s²**).

If the weight of a body located at the "standard location" is to be determined in Newton. Here measurements give **g = 9.806 m/s²** :

$$W = mg \quad (g = 9.806 \text{ m/s}^2)$$

U.S. Customary : in the U.S. Customary system of units (**FPS**) length is measured in feet (ft), time in second (s), and force in pounds (lb). The unit of mass, called a slug, is derived from **F = ma**.

TABLE 1-1 Systems of Units

Name	Length	Time	Mass	Force
International System of Units	meter	second	kilogram	newton*
SI	m	s	kg	N $\left(\frac{\text{kg} \cdot \text{m}}{\text{s}^2}\right)$
U.S. Customary FPS	foot	second	slug*	pound
	ft	s	$\left(\frac{\text{lb} \cdot \text{s}^2}{\text{ft}}\right)$	lb

*Derived unit.

TABLE 1-2 Conversion Factors

Quantity	Unit of Measurement (FPS)	Equals	Unit of Measurement (SI)
Force	lb		4.448 N
Mass	slug		14.59 kg
Length	ft		0.304 8 m

Example :

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Convert 2 km/h to m/s How many ft/s is this ?

Solution:

Since 1km = 1000 m and 1h = 3600 s , the factors of conversion are arranged in the following order, so that a cancellation of the units can be applied :

$$\begin{aligned} 2 \text{ km/h} &= \frac{2 \cancel{\text{km}}}{\cancel{\text{h}}} \left(\frac{1000 \text{ m}}{\cancel{\text{km}}} \right) \left(\frac{1 \cancel{\text{h}}}{3600 \text{ s}} \right) \\ &= \frac{2000 \text{ m}}{3600 \text{ s}} = 0.556 \text{ m/s} \end{aligned} \quad \text{Ans.}$$

From Table 1-2, 1 ft = 0.3048 m. Thus,

$$\begin{aligned} 0.556 \text{ m/s} &= \left(\frac{0.556 \cancel{\text{m}}}{\text{s}} \right) \left(\frac{1 \text{ ft}}{0.3048 \cancel{\text{m}}} \right) \\ &= 1.82 \text{ ft/s} \end{aligned} \quad \text{Ans.}$$

Example :

Convert the quantities 300 lb · s and 52 slug/ft³ to appropriate SI units.

Solution :

$$1\text{b} = 4.448 \text{ N}.$$

$$\begin{aligned} 300 \text{ lb} \cdot \text{s} &= 300 \cancel{\text{lb}} \cdot \text{s} \left(\frac{4.448 \text{ N}}{1 \cancel{\text{lb}}} \right) \\ &= 1334.5 \text{ N} \cdot \text{s} = 1.33 \text{ kN} \cdot \text{s} \end{aligned} \quad \text{Ans.}$$

Since 1 slug = 14.593 8 kg and 1 ft = 0.304 8 m, then

$$\begin{aligned} 52 \text{ slug/ft}^3 &= \frac{52 \cancel{\text{slug}}}{\cancel{\text{ft}}^3} \left(\frac{14.59 \text{ kg}}{1 \cancel{\text{slug}}} \right) \left(\frac{1 \cancel{\text{ft}}}{0.304 \text{ m}} \right)^3 \\ &= 26.8(10^3) \text{ kg/m}^3 \\ &= 26.8 \text{ Mg/m}^3 \end{aligned} \quad \text{Ans.}$$

